

1     **Southern Hemisphere extra-tropical gravity wave sources and**  
2           **intermittency revealed by a middle atmosphere General**  
3                   **Circulation Model**

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8 ABSTRACT

9 Southern Hemisphere extra-tropical gravity wave activity is examined using  
10 simulations from a free-running middle atmosphere general circulation model  
11 called Kanto which contains no gravity wave parameterizations. The total ab-  
12 solute gravity wave momentum flux (MF) and its intermittency, diagnosed by  
13 the Gini coefficient, are examined during January and July. The MF and inter-  
14 mittency results calculated from the Kanto model agree well with results from  
15 satellite limb and super-pressure balloon observations. The analysis of the Kanto  
16 model simulations indicates the following results. Non-orographic gravity waves  
17 are generated in Kanto in the frontal regions of extra-tropical depressions and  
18 around tropopause-level jets. Regions with lower (higher) intermittency in the  
19 July mid-stratosphere become more (less) intermittent by the mesosphere due  
20 to lower-level wave removal. The gravity wave intermittency is low and nearly  
21 homogeneous throughout the SH middle atmosphere during January. This in-  
22 dicates that non-orographic waves dominate at this time of year, with sources  
23 including continental convection as well as oceanic depressions. Most of the  
24 zonal-mean MF at  $40^{\circ} - 65^{\circ}\text{S}$  in January and July is due to gravity waves located  
25 above the oceans. The zonal-mean MF at lower latitudes in both months has  
26 a larger contribution from the land regions but the fraction above the oceans  
27 remains larger.

# 28 1. Introduction

29 Despite their relatively small scale, gravity waves are an important component of the  
30 atmospheric general circulation because they transfer momentum upward from tropospheric  
31 sources to the middle atmosphere. The gravity wave drag generated upon breaking closes  
32 the mesospheric jet and induces a summer to winter pole mesospheric circulation (Haynes  
33 et al. 1991; Garcia and Boville 1994). Gravity waves, together with planetary waves, drive  
34 the winter polar stratosphere away from its radiatively determined state: the existence of the  
35 winter polar stratopause itself is an indicator of strong gravity wave forcing (Hitchman et al.  
36 1989). Gravity wave driving contributes to the Quasi-Biennial Oscillation (QBO) (Sato and  
37 Dunkerton 1997; Kawatani et al. 2010; Ern et al. 2014). The temperature perturbations of  
38 gravity waves can induce the formation and affect the composition of polar stratospheric and  
39 polar mesospheric clouds when the background temperature is close to the clouds' formation  
40 thresholds (Carslaw et al. 1998; Dörnbrack et al. 2001; Shibata et al. 2003; Höpfner et al.  
41 2006; McDonald et al. 2009; Alexander et al. 2011; Kaifler et al. 2013).

42 Southern Hemisphere gravity wave sources vary seasonally and latitudinally. Higher grav-  
43 ity wave activity is observed at high southern latitudes during winter than during summer.  
44 This enhanced wave activity is due to stronger winter sources such as wave generation by  
45 fronts and jets, as well as the generation of waves from orographic sources (Yan et al. 2010;  
46 Ern et al. 2011; Alexander and Grimsdell 2013; Hendricks et al. 2014). Conversely, during  
47 summer, gravity wave activity increases in the tropical and sub-tropical regions as a result of  
48 enhanced deep convective activity and latent heat release above the continents (Jiang et al.  
49 2004; Alexander et al. 2008c). The major sources of Southern Hemisphere orographic gravity

50 waves (OGWs) visible in climatologies are the Andes and Antarctic Peninsula (e.g. Baum-  
51 gaertner and McDonald (2007); Alexander et al. (2009b); Sato et al. (2012); Geller et al.  
52 (2013)). Large OGW activity is often observed to extend significant distances downstream  
53 (leeward) from these mountainous regions, indicative of momentum flux deposition occurring  
54 significant distances from the OGW sources, and often above oceanic regions (Preusse et al.  
55 2002; Sato et al. 2012). Islands in the Southern Ocean have also been identified as sources  
56 of OGWs (Alexander et al. 2009a; Alexander and Grimsdell 2013) as well as mountainous  
57 regions in southern Africa and southern Australia (Eckermann and Wu 2012). Katabatic  
58 winds draining the interior of Antarctica can excite OGWs as they flow over topographical  
59 features (Watanabe et al. 2006; Tomikawa et al. 2015). Synoptic-scale depressions centred  
60 over the Southern Ocean direct winds onto the East Antarctic coast where they interact  
61 with katabatic winds or ice topography to produce OGWs (Orr et al. 2014; Alexander and  
62 Murphy 2015).

63 Non-orographic gravity wave (NGW) activity is large above the Southern Ocean during  
64 winter (Wu and Eckermann 2008; Alexander et al. 2009b; Hendricks et al. 2014). Observa-  
65 tions and modelling indicate that high stratospheric NGW activity and momentum flux is  
66 associated with spontaneous adjustment processes and jet instability (Plougonven and Zhang  
67 2014; Yasuda et al. 2015a,b). NGWs may also be generated through convective heating  
68 associated with frontal activity and deep convection (Fritts and Nastrom 1992; Eckermann  
69 and Vincent 1993; Tsuda et al. 1994; Alexander and Pfister 1995). Case studies using the  
70 WRF model in the Southern Ocean indicate the role of moisture and convective updrafts  
71 in generating gravity waves (Plougonven et al. 2015). Large NGW activity was observed  
72 and modelled around the sub-tropical jet (Sato 1994; Kawatani et al. 2004; Alexander et al.



2008b). Individual OGWs in the Southern Hemisphere stratosphere are responsible for the largest momentum fluxes. The NGWs do not produce the ‘hot-spot’ of activity characteristic of OGW sources, because the NGWs are emitted from sources which vary temporally and spatially. Yet the NGW sources have a lower intermittency (i. e. they occur more frequently) than the large, but less common OGW events (Plougonven et al. 2013; Wright et al. 2013). The lower intermittency of NGWs means that in the zonal mean, NGWs are responsible for a similar, albeit slightly smaller, contribution as OGWs to total momentum flux in the spring mid-stratosphere above Antarctica (Vincent et al. 2007; Hertzog et al. 2008).

General circulation models used for weather forecasting and climate research do not resolve the full spectrum of gravity waves due to their relatively coarse horizontal and vertical resolution. This is especially true for climate models, as it is computationally too expensive to run climate simulations at the very high resolution required for spontaneous wave generation. This situation is unlikely to change in the foreseeable future, therefore gravity wave parameterization schemes have been developed to include the effects on the atmosphere of the unresolved waves. Gravity wave parameterizations determine the momentum forcing of the waves on the atmosphere. These parameterizations need to be constrained by observations of momentum flux, which have been made from instruments including satellites (Ern et al. 2004; Alexander et al. 2008a; Wright et al. 2013), super-pressure balloons (Vincent et al. 2007; Hertzog et al. 2008; Plougonven et al. 2013), radars (Vincent and Reid 1983; Sato 1993; Murayama et al. 1994; Sato 1994; Alexander et al. 2008d; Dutta et al. 2008; Sato et al. 2014) and radiosondes (Sato and Dunkerton 1997; Gong et al. 2008; Murphy et al. 2014), although in each case the instruments can only measure part of the gravity wave spectrum. A parameterization of OGWs was sufficient for GCMs including only the

96 troposphere and lower stratosphere. Nowadays, with climate models increasingly more likely  
97 to include the whole stratosphere and even the mesosphere, NGWs must also be parame-  
98 terized in order to correctly represent the structure of the middle atmosphere (Alexander  
99 et al. 2010; Morgenstern et al. 2010). Non-orographic gravity waves remain challenging to  
100 parameterize in general circulation models due to the complexity of the flow in which they  
101 originate (Plougonven and Zhang 2014). NGW parameterization schemes are more com-  
102 plex than OGW parameterizations and are also complicated by the fact that the generation  
103 mechanisms of some jet-front NGWs remains unknown except for several idealized situations  
104 (Plougonven and Zhang 2014; Yasuda et al. 2015a).

105 A few high-resolution general circulation models have recently been developed which do  
106 not contain gravity wave parameterizations, that is, all waves are spontaneously generated by  
107 the model itself (Watanabe et al. 2008; Becker 2009). Such models can be used for compar-  
108 isons with observations and other models which do contain gravity wave parameterizations  
109 (Geller et al. 2013). However, gravity waves with scales around or below the size of the  
110 model resolution are likely not properly simulated by these GCMs. Results from the Kanto  
111 GCM illustrated the meridional propagation of gravity waves in the middle atmosphere,  
112 where waves in the winter hemisphere propagate poleward and upward into the core of the  
113 stratospheric polar night jet (Sato et al. 2009). These model results complement recent ob-  
114 servational evidence for meridional wave propagation in the summer and winter hemispheres  
115 (Ern et al. 2013; Hindley et al. 2015). The monthly Southern Hemisphere gravity wave  
116 activity from Kanto shows peaks associated with large mountain ranges and enhancements  
117 around the stratospheric jet (Sato et al. 2012).

118 The aim of this study is to use the Kanto model to examine the spatial and tempo-

119 ral variability of SH stratospheric momentum flux and its intermittency and determine the  
120 contribution to total SH momentum flux from oceanic and land regions during a represen-  
121 tative summer and winter month. The model data and its analysis is outlined in Section 2.  
122 The results of the gravity wave momentum flux sources and intermittency are detailed in  
123 Section 3, including zonal means, regional contributions to total momentum flux and com-  
124 posites of non-orographic gravity wave sources. Lastly, a discussion (Section 4) and summary  
125 (Section 5) are presented.

## 126 **2. Data Analysis**

127 We use data output from a free-running T213L256 atmospheric global circulation model  
128 (GCM) called Kanto, developed by Watanabe et al. (2008). No gravity wave parameteriza-  
129 tions are used in this model, thus all the gravity waves are generated spontaneously. The  
130 model time-step is 30 seconds and the horizontal resolution corresponds to a  $0.5625^\circ$  grid.  
131 Despite the lack of parameterizations, Kanto obtains realistic middle atmosphere winds and  
132 temperature structure, although the 15 month period of the QBO in the model is shorter  
133 than in reality (Watanabe et al. 2008; Kawatani et al. 2010). All physical quantities are  
134 sampled hourly. Computing the momentum flux directly from the wind perturbations would  
135 require saving model output at very high temporal resolution ( $\sim 5$  minutes) in order to  
136 perform the desired spectral analysis. As saving the model output at this resolution is not  
137 practical, an alternative method must be used to compute momentum flux from this hourly  
138 resolution data. We follow the approach described in Geller et al. (2013) to estimate the  
139 square of the total absolute gravity wave momentum flux as:

$$\begin{aligned}
\mathbf{M}^2 &= \left(1 - \frac{f^2}{\hat{\omega}^2}\right)^2 \rho_0^2 [(\overline{u'w'})^2 + (\overline{v'w'})^2] \\
&= \rho_0^2 \overline{w'^2} (\overline{u'^2} + \overline{v'^2}) \left(1 - \frac{f^2}{\hat{\omega}^2}\right)^2 \left(1 + \frac{f^2}{\hat{\omega}^2}\right)^{-1}
\end{aligned} \tag{1}$$

141 where

$$\frac{f^2}{\hat{\omega}^2} \approx \left(\frac{fg}{N^2 T_0}\right)^2 \frac{\overline{T'^2}}{\overline{w'^2}}$$

142 The  $T_0$  and  $\rho_0$  are the background temperature and densities, which are calculated from the  
143 large-scale flow. For this analysis, we filter the data to retain components which have a total  
144 horizontal wavenumber  $n$  of less than six and define this as the background. The primes  
145 indicate gravity wave perturbations which we define as waves with  $n > 21$ , which is the same  
146 cut-off as used previously by Sato et al. (2009, 2012).

147 Gravity wave activity varies through time and in particular, OGWs are known to occur  
148 infrequently although they can be of very large magnitudes (Plougonven et al. 2008). In  
149 addition to knowledge of the mean values of gravity wave activity over various regions, it  
150 is desirable to know whether the wave field is dominated by a few large events (such as  
151 for OGWs) or has a more continuous emission (likely for NGWs). This is quantified by  
152 diagnosing the intermittency of the gravity wave field. The intermittency may be defined  
153 by, for example, the proportion of time that the mean is exceeded (Sato et al. 2012) or  
154 the ratio of the 50th to 90th momentum flux percentiles (Hertzog et al. 2008). Here, we  
155 follow Plougonven et al. (2013) by using the Gini coefficient to define the intermittency of  
156 the gravity wave momentum fluxes. For a series containing  $M$  samples, we have for the  
157  $m$ th sample a momentum flux of  $\mathbf{M} = \mu_m$ , calculated via Equation 1. Assuming that the

158 momentum fluxes are sorted into increasing order (with  $1 \leq m \leq M$ ), the cumulative sum  
 159 is expressed as  $F_m = \sum_{i=1}^m \mu_i$ . The mean is expressed as  $\bar{\mu} = F_M/M$ . The intermittency is  
 160 determined via:

$$I = \frac{\sum_{m=1}^{M-1} (m\bar{\mu} - F_m)}{\sum_{m=1}^{M-1} m\bar{\mu}} \quad (2)$$

161 The  $I$  will vary between 0 (no intermittency, constant series) and 1 (most intermittent).  
 162 This method has the advantage of using integration so it is less susceptible to sampling; and  
 163 this method also avoids a somewhat arbitrary choice of limits.

164 Kanto was run for three model years, with each year having a length of 360 days and  
 165 each of the twelve months consisting of 30 days. We analyze data from the three Januarys  
 166 and three Julys to determine the seasonal changes in gravity wave activity and intermittency  
 167 in the Southern Hemisphere. The January and July output are consistent with the typical  
 168 seasonal evolution of the general circulation in the middle atmosphere (Watanabe et al.  
 169 2008).

## 170 3. Results

### 171 a. Momentum flux and intermittency

172 Figure 1 illustrates the January and July zonal-mean total absolute gravity wave mo-  
 173 mentum flux (MF) and zonal-mean zonal wind in the Southern Hemisphere. The vectors  
 174 indicate the meridional and vertical wave potential energy flux ( $\rho_0 \overline{\phi'v'}$ ,  $\rho_0 \overline{\phi'w'}$ , where  $\phi'$  is

175 the geopotential height perturbation for  $n > 21$ ) which are parallel to the intrinsic group ve-  
176 locity of the gravity waves (see e. g. Kawatani et al. (2009); Sato et al. (2012)). The January  
177 zonal-mean zonal winds are westward above the middle stratosphere at all latitudes. The  
178 largest MF in the lower stratosphere is located equatorward of  $40^\circ\text{S}$  but diminishes rapidly  
179 with altitude as the eastward winds weaken and turn westward. In the upper stratosphere,  
180 the MF is largest at low latitudes and decreases poleward. Upward propagating waves are  
181 evident equatorward of  $\sim 30^\circ\text{S}$ .

182 The zonal-mean MF structure in the middle atmosphere is markedly different during July  
183 (Figure 1b). At increasingly higher altitudes in the stratosphere, the large lower stratospheric  
184 sub-tropical (equatorward of  $\sim 30^\circ\text{S}$ ) MF decreases as zonal wind speeds decrease. The peak  
185 MF shifts upward and poleward into the stratospheric polar night jet core. Gravity waves  
186 propagate upward and poleward from the sub-tropical jet region and are focused into the core  
187 of the polar night jet (Dunkerton 1984; Senf and Achatz 2011). Waves at higher latitudes  
188 (around  $70^\circ\text{S}$ ) propagate nearly vertically through the middle atmosphere.

189 The 50 hPa horizontal distribution of the January and July mean MF are shown in Fig-  
190 ure 2. The January 50 hPa MF distribution generally decreases poleward with slightly larger  
191 MF centred above the continents and New Zealand and extending over their surrounding  
192 oceans. The slightly larger MF in the sub-tropics above Africa, northern Australia and sub-  
193 tropical South America are likely due to gravity waves emitted by large-scale convection and  
194 are qualitatively in agreement with observations of gravity waves attributed to convective  
195 sources (Jiang et al. 2004; Alexander et al. 2008c; Ern and Preusse 2012). During July, large  
196 MF is present above the southern Andes and the Antarctic Peninsula. Over the ocean, the  
197 largest mean MF are above the southern Indian Ocean. Small, local peaks in MF are also

198 visible above topography in New Zealand, Eastern Australia, Tasmania and Southern Africa.  
199 These localised regions of enhanced gravity wave activity are also seen frequently in satellite  
200 observations (Eckermann and Wu 2012; Hendricks et al. 2014).

201 By upper stratospheric altitudes (as shown by the 1 hPa MF distributions in Figure 3),  
202 the MF has decreased in both seasons. The January peak MF is now located to the east (i.  
203 e. upwind) of Southern Africa, New Zealand and South America. The peak MF in July at  
204 1 hPa is above the southern Andes, while the second peak is above Southern Ocean, near the  
205 maximum zonal wind speeds. The MF has decreased further by 0.1 hPa, in the mesosphere,  
206 (Figure 4), although the distributions are broadly similar to those at 1 hPa with largest  
207 January MF in the sub-tropics and to the east of the continents; and largest July MF above  
208 the Southern Ocean and southern Andes.

209 Figure 5 shows the intermittency at 50 hPa. Waves produced above all the mountainous  
210 regions are highly intermittent in July. Gini coefficients range from about 0.6 above Eastern  
211 Australia, southern Africa and New Zealand to  $\sim 0.8$  above the Antarctic Peninsula. The  
212 Gini coefficients above the Andes are 0.6 – 0.7. In contrast, the coefficients above the  
213 oceans are lower, typically 0.45 – 0.55. The highest intermittency (i. e. Gini coefficient  
214  $\sim 0.8$ ) at 50 hPa is above the Trans-Antarctic mountains and the Antarctic Peninsula: these  
215 regions have lower monthly mean MF compared with lower-latitude mountainous regions (see  
216 Figure 2b). Smaller mountain ranges, such as those in New Zealand, Eastern Australia and  
217 southern Africa produce a more intermittent spectrum than their immediate surroundings.  
218 There is a higher intermittency for waves above the southern Indian ocean than above other  
219 ocean areas. The January intermittency, in contrast to July, is nearly uniform across the  
220 entire Southern Hemisphere, with Gini coefficients of 0.45 – 0.55 present above land and

221 ocean.

222 The intermittency in the July mesosphere (0.1 hPa) has changed from that in the mid  
223 stratosphere and is shown in Figure 6. The intermittency has become more uniform across  
224 the Southern Hemisphere, with increases above the oceans (coefficients of  $\sim 0.5 - 0.6$ ) and  
225 decreases above mountains (coefficients of  $0.6 - 0.65$ ) when compared with Figure 5b. The  
226 Gini coefficients calculated from the Kanto model are broadly consistent with those obtained  
227 from observations (Plougonven et al. 2013; Wright et al. 2013) and will be compared in detail  
228 below.

229 *b. Regional contributions to total momentum flux*

230 We divide the Southern Hemisphere domain into several land and oceanic regions, in  
231 order to examine the properties of total momentum flux and intermittency of each region  
232 separately. The regional boundaries are illustrated in Figure 7. This division into land  
233 and oceanic regions provides a convenient proxy for GW source attribution. We follow  
234 the Antarctic boundaries of Plougonven et al. (2013) and note that these boundaries are  
235 appropriate in Kanto too, given the structure of the MF at various altitudes (Figure 2 –  
236 Figure 4) and the wave intermittency (Figure 5). Based on analyses of the location of the  
237 sub-tropical jet (e. g. Sato et al. (2000)), we divide the oceans into the Southern Ocean and  
238 Temperate Oceans (the latter consisting of the South Atlantic, South Pacific and southern  
239 Indian Oceans) at  $45^\circ\text{S}$ . Isolated Southern Ocean islands are combined into the Southern  
240 Ocean region because Kanto does not resolve the islands sufficiently. A large region above  
241 the South Atlantic is included in South America, which allows for the horizontal propagation



242 of OGW wave trains observed and modelled downwind of the Andes (Preusse et al. 2002;  
243 Sato et al. 2012). For the same reason, Drake Passage and South Georgia also form part of  
244 South America (see Figure 3).

245 The 50 hPa zonal-mean MF above all land and all oceans are illustrated in Figure 8c  
246 and Figure 8d for January and July respectively, along with the total zonal-mean MF. The  
247 zonal-mean MF above land and ocean are normalized by the fraction at each latitude which  
248 consists of land and ocean, respectively. The total zonal-mean MF from  $\sim 40^{\circ}\text{S} - 65^{\circ}\text{S}$  is  
249 mainly due to contributions from oceanic regions. Further north, the land regions contribute  
250 a larger fraction of total zonal-mean MF, although the contribution from above the ocean  
251 is still larger. From  $65^{\circ}\text{S} - 70^{\circ}\text{S}$ , only a small ocean region exists off the coast of West  
252 Antarctica (see Figure 7) so in this latitude band, the zonal-mean MF above land is around  
253 twice as large as that above the ocean. The peak in MF in July occurs at around  $40^{\circ}\text{S} - 50^{\circ}\text{S}$   
254 and decreases equatorward. The equatorward increase of MF in January is an indication  
255 of the presence of non-orographic gravity wave sources such as convection. Both the land  
256 and ocean zonal-mean MF are much lower at 0.1 hPa in January (Figure 8a) and July  
257 (Figure 8b), but retain similar relative contributions to total zonal MF as at 50 hPa.

258 The regional mean MF as a function of altitude is illustrated for January and July in  
259 Figure 9. The July mean MF at 100 hPa above the temperate oceans is larger than above  
260 the Southern Ocean but smaller above about 50 hPa. This is probably due to polarward  
261 propagation of waves and partly due to dissipation near the sub-tropical weak wind layer  
262 around 50 hPa (see Figure 1b). MF above all regions decrease with altitude, with the rate  
263 of decrease similar above land and oceanic regions. The large July mean MF above the  
264 Southern Ocean, South America and the Antarctic Peninsula is visible in Figure 9b, while

265 the large January mean MF above land regions is visible in Figure 9a throughout the middle  
266 atmosphere.

267 The vertical profile of the mean intermittency (expressed as the Gini coefficient) in each  
268 region is presented in Figure 10. The intermittency is essentially constant with altitude  
269 during January for all regions ( $\sim 0.5$ ). In contrast, the intermittency during July varies  
270 with altitude and its behavior depends upon the region. For regions with low intermittency  
271 ( $< 0.55$ ) below 30 hPa, the intermittency increases with altitude. The intermittencies above  
272 the Antarctic Peninsula, Coastal Antarctica and South America initially increase before  
273 decreasing by the 3 hPa pressure level and at 0.1 hPa are comparable with most other  
274 regions. The relatively low mean South American intermittency is a result of the large area  
275 of this region (see Figure 7).

276 *c. Non-orographic gravity wave sources and propagation*

277 Convective heating associated with extra-tropical depressions and frontal activity are  
278 sources of NGWs (Plougonven et al. 2013). To explore the general behaviour of convective  
279 NGW sources in Kanto, the July composite 580 hPa root-mean-squared (rms) horizontal  
280 wind divergence of oceanic-region depressions is shown in Figure 11a. To form this compos-  
281 ite, oceanic-region depressions which have local minimum altitudes in the 850 hPa geopo-  
282 tential surface field of  $< 1300$  m are identified (the composite mean geopotential height is  
283 indicated by the black contour lines on Figure 11). The algorithm finds depressions satisfy-  
284 ing these criteria at each hourly model time step. The results are not overly sensitive to the  
285 choice of these limits. The resulting composite mid-tropospheric (580 hPa) horizontal wind

286 divergence field is maximum above the frontal region, where precipitation is locally maxi-  
287 mum. Gravity waves are emitted from the frontal region (coincident with the precipitation  
288 extending north of the composite depression's center) rather than from the actual center  
289 where precipitation is maximum. This indicates that fronts are the main source of waves  
290 associated with depressions in the Kanto model. The divergence field north of the depression  
291 has spread out at 200 hPa (Figure 11b) compared with the mid-troposphere, while a local  
292 minimum in divergence exists around and to the west of the composite depression's center.  
293 Some of the gravity waves generated by these depressions are probably filtered at pressure  
294 levels below 200 hPa, while some propagate and interact with jet-emitted waves.

295 The other source of extra-tropical NGWs are spontaneous adjustment processes and jet  
296 instability. We examine a case of two vertical cross-sections of the divergence field through  
297 a depression located in the South Atlantic. The wavelike structures evident in Figure 12  
298 provide information about wave properties and source characteristics in Kanto, which is  
299 important for a better understanding of the mean distribution of gravity waves. Convergence  
300 and divergence with downward tilting phase fronts occur below the jet core and upward  
301 tilting phase fronts occur above the jet core (Figure 12b, around 200 hPa at  $10^{\circ}\text{W} - 10^{\circ}\text{E}$ ).  
302 This phase structure indicates that the jet itself is the source of these waves. Some of these  
303 waves can be easily followed upward to 30 hPa. Phase fronts in the latitude cross-section  
304 (Figure 12a) are also seen above about 100 hPa, tilting upward and initially equatorward,  
305 although toward 30 hPa the divergence field is only large in the strong zonal wind region of  
306 the stratospheric polar jet.

307 The composite of the middle atmosphere momentum flux of the oceanic NGWs produced  
308 through upper tropospheric jet mechanisms is investigated by examining it relative to the

309 cores of the sub-tropical jet (STJ, temperate ocean region) at 200 hPa and the polar-front  
310 jet (PFJ, Southern Ocean region) at 300 hPa during July. For each model time-step, data  
311 are extracted at longitudes where the horizontal wind speed at 200 hPa (STJ) or 300 hPa  
312 (PFJ) is locally maximum and exceeds  $50 \text{ m s}^{-1}$ . The resultant July composites are shown  
313 in Figure 13 and allow us to examine wave propagation through the middle atmosphere  
314 relative to the location of the jet source. The MF decreases with height most quickly on the  
315 equatorward flank of the STJ (Figure 13a; positive relative latitudes) as the gravity waves  
316 propagate into a region of decreasing horizontal wind speed in the middle stratosphere. Such  
317 structure in the absolute value of MF is consistent with the concept of critical-level removal  
318 of gravity waves by the background winds, leaving fewer waves to propagate to successively  
319 higher altitudes. In contrast, the MF above the poleward side of the sub-tropical jet decreases  
320 less rapidly. The gravity waves from the STJ are directed upward and poleward into the  
321 core of the polar stratospheric jet.

322 Above the Southern Ocean (Figure 13b), the composite of the PFJ indicates an upward  
323 motion of gravity waves and their momentum flux into the core of the polar stratospheric  
324 jet. The poleward-directed vectors in the lower stratosphere on the equatorward flank of the  
325 PFJ (positive relative latitudes) indicate that some of these waves are propagating southward  
326 from the STJ. This contrasts with the nearly vertical propagation of waves on the poleward  
327 side of the PFJ.

## 328 4. Discussion

329 The horizontal distributions of MF at 50 hPa, 1 hPa and 0.1 hPa calculated from the  
330 Kanto model output data (Figures 2 – 4) may be compared with estimates of MF from  
331 satellite and super-pressure balloon observations and with models which use gravity wave  
332 parameterizations. It is worth emphasising here that the Kanto model data and the satellite  
333 observations are sensitive to overlapping but not identical parts of the gravity wave spectrum  
334 (i. e. each having its own observational window (Alexander et al. 2010)). Furthermore,  
335 differences in satellite data processing algorithms result in different zonal-mean MF (see  
336 Figure 1 of Geller et al. (2013) regarding HIRDLS).

337 Limb-scanning satellites such as CRISTA and HIRDLS provide vertical profiles of tem-  
338 perature along the orbit track. Horizontal wavelengths are estimated from adjacent profiles,  
339 although they remain undersampled (Ern et al. 2004; Alexander et al. 2008a). Absolute  
340 values of momentum fluxes are then estimated by combining the horizontal and vertical  
341 wavelengths with the temperature perturbations of the gravity waves, although these MF  
342 are likely biased low due to uncertainties in the horizontal wavelengths (Preusse et al. 2009).  
343 Monthly mean MF in the lower stratosphere around 25 km altitude above the southern tip  
344 of South America during May and August 2006 was around 5 mPa as measured by HIRDLS  
345 (Alexander et al. 2008a, 2010) and SABER (Ern et al. 2011), but about 30 mPa during  
346 August 1997 as measured by CRISTA data (Ern et al. 2004). The HIRDLS and SABER  
347 results compare favorably with the July Kanto MF at 50 hPa of 4 – 5 mPa (Figure 2b).  
348 In the zonal mean, all three satellites show similar features during August with the largest  
349 MF centered at 55°S, similar to the zonal-mean MF in July in Figure 1. Ern et al. (2011)

350 also reported larger January MF above the sub-tropical continents than above the oceans  
351 (monthly means of about 1 – 2 mPa above land at 30 km), consistent with the 50 hPa Kanto  
352 results in Figure 2a.

353 Long-duration super-pressure balloons (the Vorcore campaign) were launched in Antarc-  
354 tica during spring 2005, with the last flight terminating in February 2006. These balloons  
355 travelled on isopycnic surfaces (equivalent to  $\sim 18$  km altitude) around Antarctica and the  
356 Southern Ocean and provide detailed information on gravity wave sources, intermittency and  
357 MF (Hertzog et al. 2008). The Vorcore zonal-mean density-weighted momentum fluxes in the  
358 direction of wave propagation  $\overline{\rho_0 u'_{\parallel} w'}$  were calculated above orographic and non-orographic  
359 regions (some areas, like the East Antarctic plateau, were classified as non-orographic due  
360 to their flat topography). Hertzog et al. (2008) demonstrated that about two thirds of total  
361 zonal-mean MF south of 70°S was present above mountainous areas. On the other hand,  
362 between 45°S and 70°S, the vast majority of zonal-mean MF was due to MF located above  
363 oceanic regions. This dominance in the zonal mean of MF above the Southern Ocean is also  
364 present in Kanto during January and July (Figure 8). Furthermore, the proportion of ocean  
365 to land zonal-mean MF in both January and July is similar at 50 hPa and 0.1 hPa. While  
366 individual orographic gravity waves have very large MF, their high intermittency and the  
367 localised land areas diminish their importance in the zonal mean. The Kanto results extend  
368 further north than the Vorcore observations. Equatorward of  $\sim 40^\circ$ S, the land regions con-  
369 tribute towards half of the total zonal-mean MF in July at 50 hPa. This is due to the larger  
370 MF above the Andes at these latitudes, along with small contributions from other orography  
371 countering the weaker MF above the temperate oceans (Figure 2). Both Vorcore and Kanto  
372 in January show a general decrease of total zonal-mean MF poleward and the Kanto total

373 zonal-mean MF is similar in magnitude to the Vorcore data.

374 The Kanto July intermittency (Figure 6 and Figure 10) converges with altitude toward  
375 near-uniform values of 0.5 – 0.6 at 0.1 hPa across the SH extra-tropics, with intermittency  
376 above orography reducing from the lower stratosphere, but intermittency above the oceans  
377 increasing. Such results can be understood readily by considering the intervening filtering  
378 of both NGWs and OGWs, as described in detail by Wright et al. (2013). The decreasing  
379 zonal wind speeds with altitude in the sub-tropics will remove waves with lower phase speeds  
380 resulting in a more intermittent spectrum. Conversely, OGWs will be removed when the  
381 background wind is close to zero, reducing the intermittency. While in July the zonal-mean  
382 wind speeds are positive throughout the middle atmosphere (Figure 1b), individual wind  
383 profiles where the wind direction changes by more than  $180^\circ$  between source and observing  
384 height result in OGW removal (e. g. Baumgaertner and McDonald (2007); Alexander et al.  
385 (2013)). The intermittency (expressed as the Gini coefficient) above the Antarctic Peninsula  
386 and southern Andes during July at 50 hPa is 0.6 – 0.8 and above the oceans it is 0.45 – 0.55  
387 (Figure 5), while the whole SH has Gini coefficients of  $\sim 0.5$  in January. These compare with  
388 Gini coefficients of 0.6 – 0.7 above the Antarctic Peninsula reported by Plougonven et al.  
389 (2013) from super-pressure balloon observations made during spring. Using three years of  
390 HIRDLS data, Wright et al. (2013) showed higher zonal-mean Gini coefficients in winter  
391 than in summer in the SH extra-tropics, along with a convergence of the Gini coefficient  
392 with increasing altitude (i. e. a less intermittent wave spectrum). The Kanto results of  
393 Figure 10 are similar to the HIRDLS observations, although the Kanto Gini coefficients are  
394 larger which may be due to longer averaging (across all seasons) in HIRDLS.

395 The low intermittency reported in the January lower stratosphere ( $\sim 0.5$ , see Figure 5a)

396 indicates the dominance of non-orographic wave sources. Furthermore, while the phase  
397 speeds of orographic gravity waves vary from zero in a time-varying flow (e. g. Chen et al.  
398 (2005)), the majority of mountain waves produced during January will encounter their crit-  
399 ical levels due to the lower stratospheric wind reversal present at this time. The non-zero  
400 January zonal-mean MF above land is largely a result of gravity wave emission from deep  
401 convective activity above the mid-latitude and sub-tropical land masses. The zonal-mean MF  
402 above the land and ocean regions presented in Figure 8 provide insights into wave sources and  
403 propagation in the Kanto model throughout the SH middle atmosphere. Orographic gravity  
404 waves may propagate upward above the land through the middle atmosphere during winter  
405 until they break at high altitudes. Eastward propagating depressions produce non-stationary  
406 non-orographic gravity waves prior to, during and after encountering the Andes (Sato et al.  
407 2012). The July zonal-mean MF above the land is a combination of orographic gravity waves  
408 and non-orographic gravity waves from these synoptic depressions. The orography in Kanto  
409 is smoothed from that in reality (and several Southern Ocean islands are not resolved by  
410 the model), so the MF generated by the Kanto orography is likely underestimated compared  
411 with observations. Despite this smoothed orography, gravity wave temperature perturba-  
412 tions above the Andes in the lower stratosphere in Kanto reach 2 – 3 K (not shown), similar  
413 to that reported in satellite observations (e. g. Eckermann and Preusse (1999)).

414 Many global circulation models (GCMs) do not have spontaneous wave generation, rather  
415 they use a gravity wave parameterization scheme to produce a realistic middle atmosphere  
416 circulation. During summer, GCMs with gravity wave parameterizations have larger MF  
417 over Antarctica than those seen in observations and with Kanto (Geller et al. 2013), which  
418 tend toward zero MF toward the South Pole. These discrepancies were attributed to the



419 source flux specifications in the parameterization schemes (Geller et al. 2013).

420 Various source mechanisms for the production of extra-tropical non-orographic gravity  
421 waves have been proposed following observations and idealized simulations. Recent super-  
422 pressure balloon observations and modelling results indicate that convective updrafts con-  
423 nected to frontal systems produce high intrinsic frequency waves above the ocean (Plougonven  
424 et al. 2015). Large mid-tropospheric horizontal divergence occurs in Kanto in the frontal  
425 zone north of the depression’s center (Figure 11a). The absence of horizontal wind diver-  
426 gence above the depression’s center, where precipitation maximises, indicates that in Kanto,  
427 gravity waves are mainly generated in the frontal zone. The strong tropopause-level jets,  
428 which are meteorologically linked to these fronts, are themselves a strong source of grav-  
429 ity waves (Figure 12). Gravity waves generated by the tropopause jets propagate into the  
430 stratosphere relatively easily (Figure 12 and Figure 13).

431 Coherent structures of gravity waves around the tropopause-level jet were evident in  
432 Figure 12. Using the Kanto data, we estimate the gravity wave parameters of the wave  
433 packet located above the core of the jet in Figure 12a (and using additional information  
434 provided by other Kanto data - not shown). The resultant gravity wave parameters are  
435 summarised in Table 1. While the zonal phase speed  $c_x$  is quite large, the background wind  
436 is also large, so that the intrinsic zonal phase speed  $\hat{c}_x = 9 \text{ m s}^{-1}$ . The horizontal and vertical  
437 wavelengths of this wave are similar to those reported in previous model and observational  
438 examples of waves generated around the jet (Guest et al. 2000; Plougonven et al. 2003;  
439 Kawatani et al. 2004; Watanabe et al. 2008; Murphy et al. 2014).

440 The results presented here all consider the total absolute value of momentum flux, rather  
441 than the zonal and meridional momentum fluxes, due to the hourly saved Kanto data reso-

442 lution. Ideally,  $\overline{u'w'}$  and  $\overline{v'w'}$  are preferable in that they provide directional information on  
443 the gravity wave forcing of the background atmosphere. Models respond to the divergence  
444 of the gravity waves' zonal and meridional momentum fluxes through its deposition into the  
445 background flow. However, as argued by Geller et al. (2013), important information about  
446 the state of the atmosphere can still be deduced by considering these total absolute values  
447 and this provides a mechanism for comparing models with observations.

## 448 5. Conclusion

449 The spatial and temporal variability of total momentum flux (MF) in the Southern  
450 Hemisphere (SH) extra-tropics was examined using the free-running Kanto GCM. Kanto  
451 does not have any gravity wave parameterizations, thus all gravity waves are spontaneously  
452 generated by the model itself. The seasonal changes in MF were examined by investigating  
453 model output in the representative months of January and July (Watanabe et al. 2008). We  
454 examine the absolute value of total momentum flux as described by Geller et al. (2013) and  
455 diagnose gravity wave intermittency with the Gini coefficient (Plougonven et al. 2013).

456 The Kanto model results indicate the presence of large, intermittent (Gini coefficients of  
457  $0.6 - 0.8$ ) MF in the middle atmosphere above orography during July. Large, less intermittent  
458 (coefficients  $< 0.55$ ) MF also occur above the Southern Ocean storm tracks during July.  
459 Larger MF is present above land than above the oceans during January throughout the  
460 middle atmosphere. The entire SH at 50 hPa has near-uniform Gini coefficients of  $\sim 0.5$  in  
461 January, indicating that the dominant wave sources are non-orographic, such as summertime  
462 continental convection. The results from the Kanto model are consistent with the magnitude

463 and locations of absolute momentum flux determined from satellite limb and super-pressure  
464 balloon observations.

465 The SH is divided into oceanic and land regions, the latter regions including some seas  
466 downwind of major orography. Most of the zonal-mean MF at  $40^\circ - 65^\circ\text{S}$  is due to gravity  
467 waves above the oceans. The January mean intermittency in each region remains constant  
468 (about 0.50) throughout the middle atmosphere. In July, regions with low intermittency in  
469 the mid-stratosphere become more intermittent with altitude. In contrast, regions with high  
470 intermittency in the mid-stratosphere (the Antarctic Peninsula, Coastal Antarctic and South  
471 America) become less intermittent by the lower mesosphere. Such results can be understood  
472 by considering the removal of different types of gravity waves with altitude, resulting in a  
473 more homogeneous intermittency in the SH at 0.1 hPa than at 50 hPa.

474 Fronts are the main source region of non-orographic gravity waves associated with depres-  
475 sions above the extra-tropical SH oceans in Kanto. Gravity waves are primarily emitted from  
476 fronts, rather than the actual depression centers where precipitation is maximum. Gravity  
477 waves are also emitted around the tropopause-level jets in Kanto. Above the oceans, non-  
478 orographic gravity waves from the sub-tropical jet propagate upward and poleward into the  
479 core of the polar stratospheric jet during July, while waves from the polar-front jet propagate  
480 nearly vertically into the stratosphere.

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708 **List of Tables**

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711 50 – 100 hPa.

34



TABLE 1. Gravity wave parameters for the wave present above the jet in Figure 12a. The  $\bar{u}$  and  $N$  are calculated over the region  $20^\circ\text{W} - 10^\circ\text{W}$ ,  $37^\circ\text{S} - 47^\circ\text{S}$  and 50 – 100 hPa.

$\lambda_x$ (km)	$\lambda_z$ (km)	$ f/\hat{\omega} $	$c_x$ (m s <sup>-1</sup> )	$\hat{c}_x$ (m s <sup>-1</sup> )	$\bar{u}$ (m s <sup>-1</sup> )	$N$ (s <sup>-1</sup> )
1000	3.5	0.3	52	9	43	0.014

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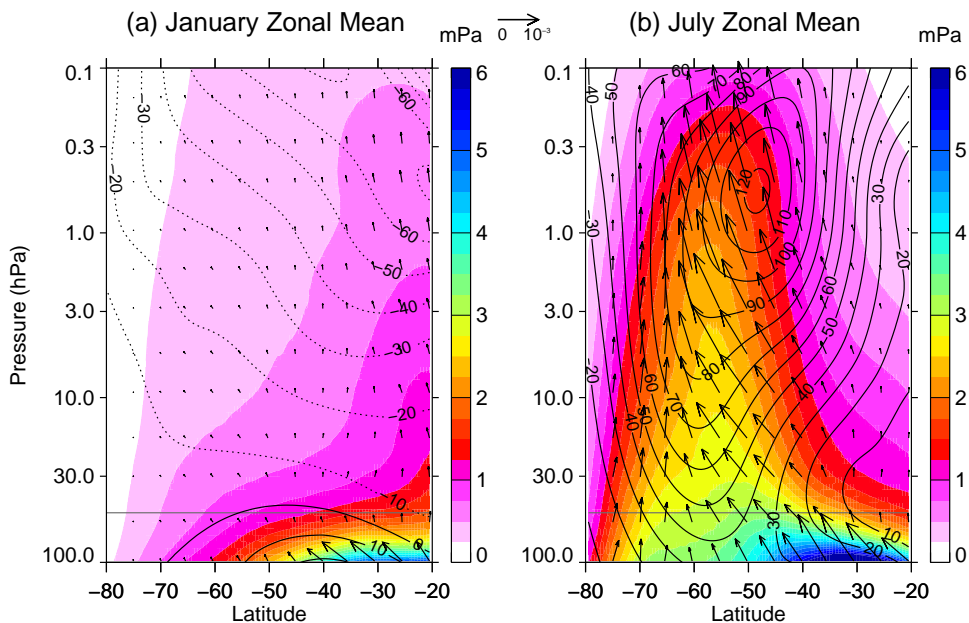


FIG. 1. The zonal-mean MF (color contours) and zonal-mean zonal wind (line contours, units of  $\text{m s}^{-1}$ , dashed lines indicate westward winds) for (a) January and (b) July. Vectors indicate the meridional and vertical wave potential energy flux ( $\rho_0 \overline{\phi'v'}$ ,  $\rho_0 \overline{\phi'w'}$ ). Vector lengths are constant between sub-panels with the magnitude given by the horizontal vector in the middle (units of  $\text{kg m}^{-1} \text{s}^{-2}$ ). The  $\rho_0 \overline{\phi'w'}$  are multiplied by a factor of 20 for clarity. The horizontal gray lines in each panel indicate 50 hPa.

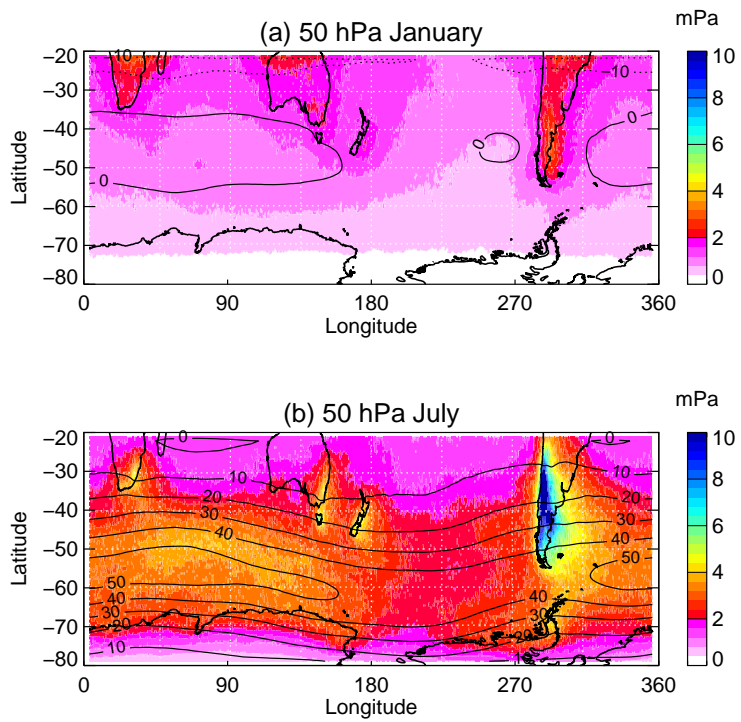


FIG. 2. The mean MF (color) and zonal wind (black lines, units of  $\text{m s}^{-1}$ , westward dashed) at 50 hPa for (a) January and (b) July. The July MF above the Andes reach 20 mPa but the contour scale is clipped at 10 mPa to resolve details above other regions.

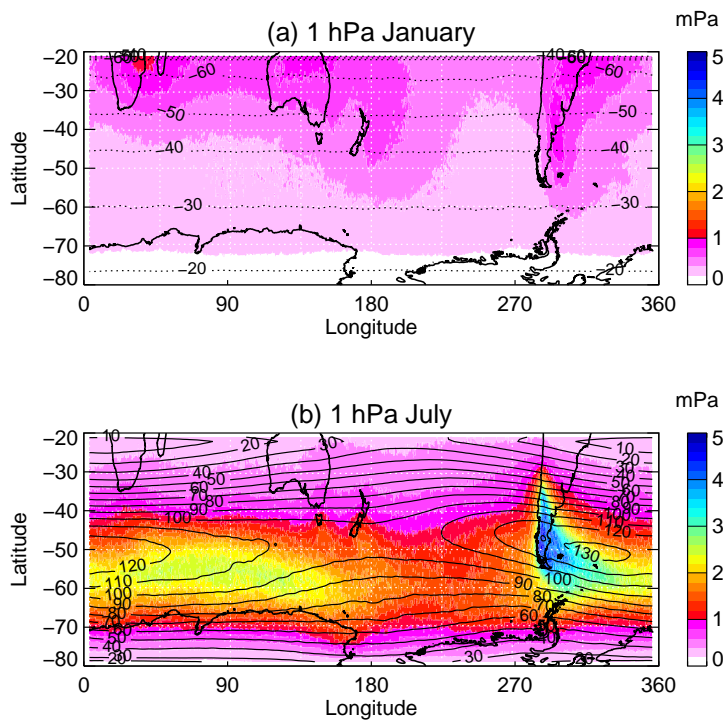


FIG. 3. As for Figure 2 but at 1 hPa.

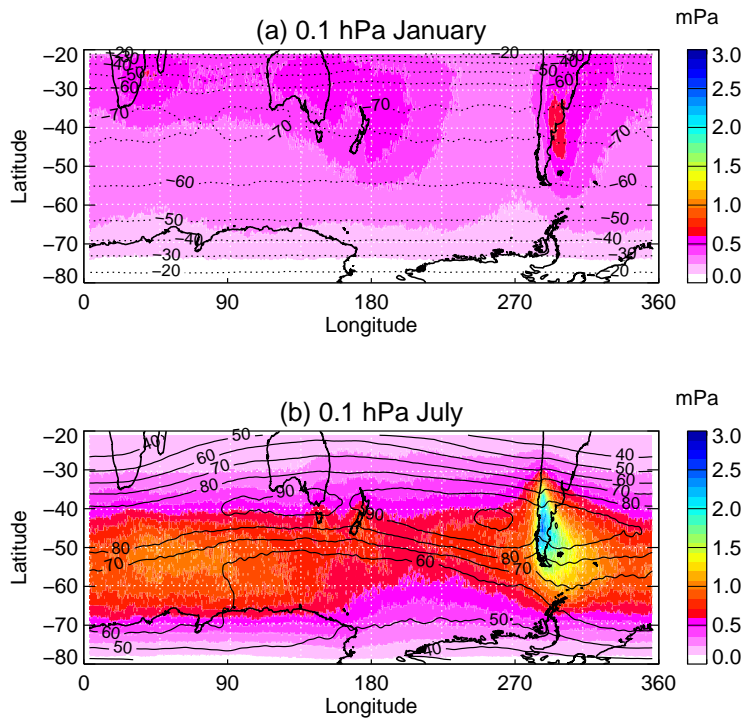


FIG. 4. As for Figure 2 but at 0.1 hPa.



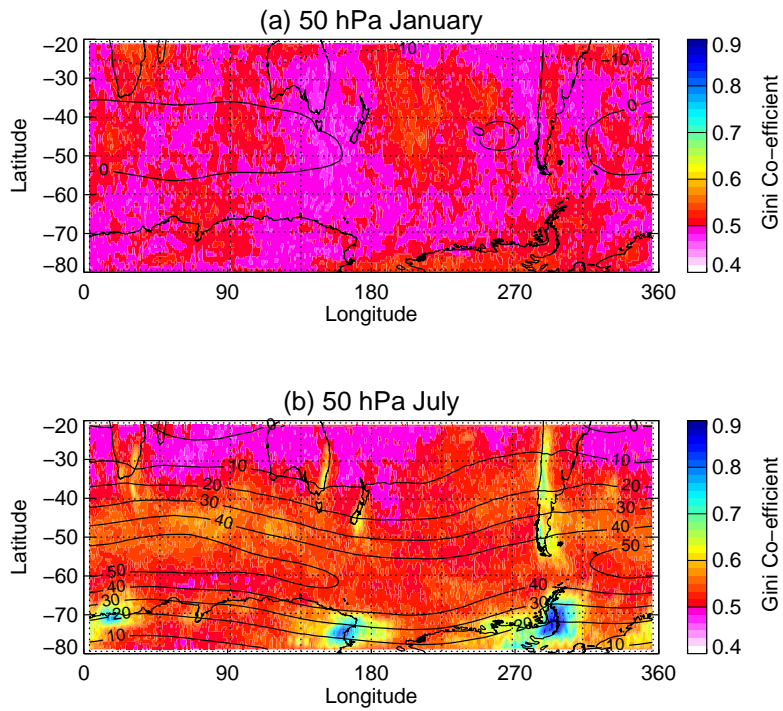


FIG. 5. The intermittency of the absolute momentum fluxes, expressed as the Gini coefficient, at 50 hPa for (a) January and (b) July. Mean zonal wind speeds are also indicated (westward dashed, units  $\text{m s}^{-1}$ ).

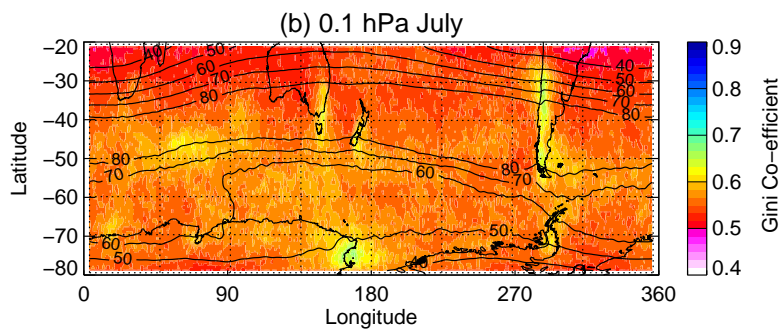


FIG. 6. The same as Figure 5 but for the 0.1 hPa intermittency during July.

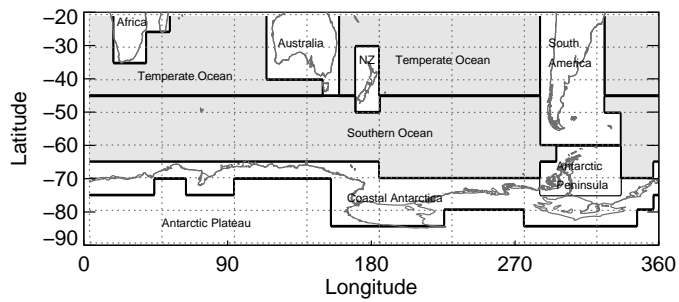


FIG. 7. Regional boundaries for the decomposition of the Southern Hemisphere extra-tropics into oceanic and land-based regions. The Indian, South Pacific and South Atlantic oceans north of  $45^\circ$  are combined into one Temperate Ocean region. Grey shading indicates regions classified as oceanic regions, while white indicates land regions.

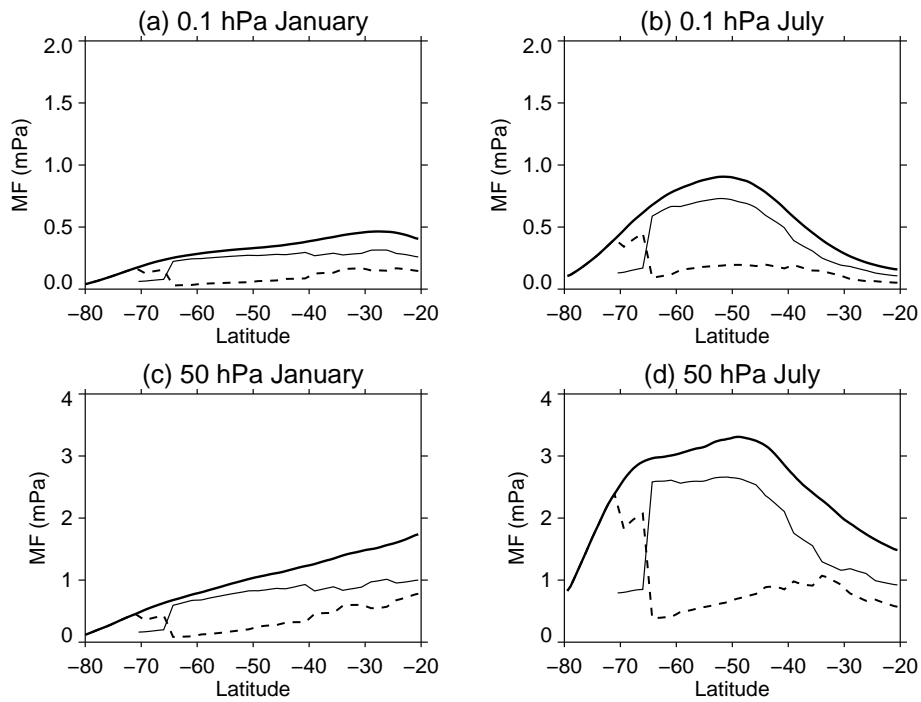


FIG. 8. January and July zonal-mean MF for the land (dashed) and oceanic (thin solid) regions at (a,b) 0.1 hPa and (c,d) 50 hPa. The thick solid line is the total MF. Note the different scales between the 50 hPa and 0.1 hPa pressure levels.

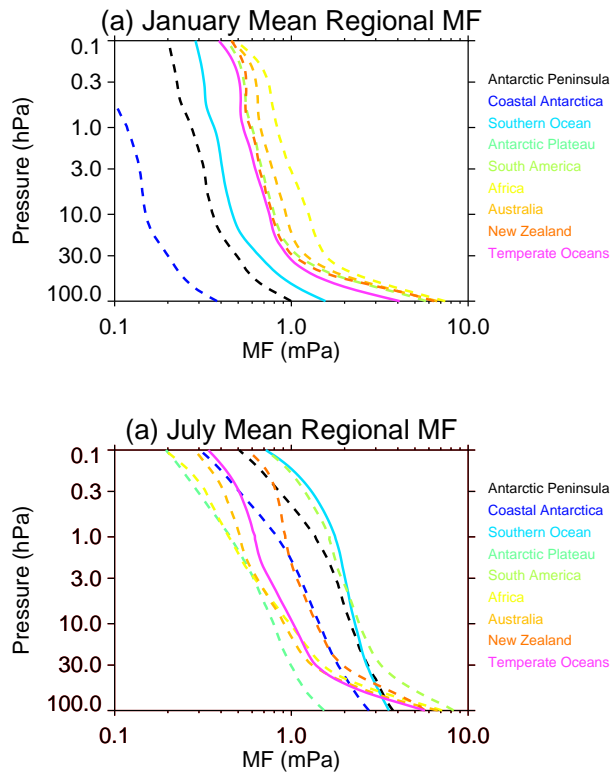


FIG. 9. Mean MF as a function of pressure level for each region for (a) January and (b) July. Solid lines indicate oceanic regions, while dashed lines indicate land regions.

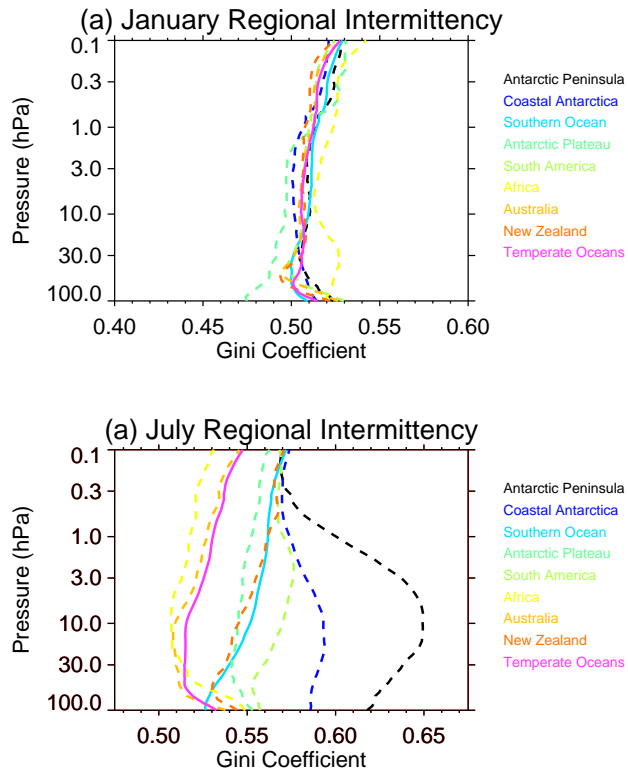


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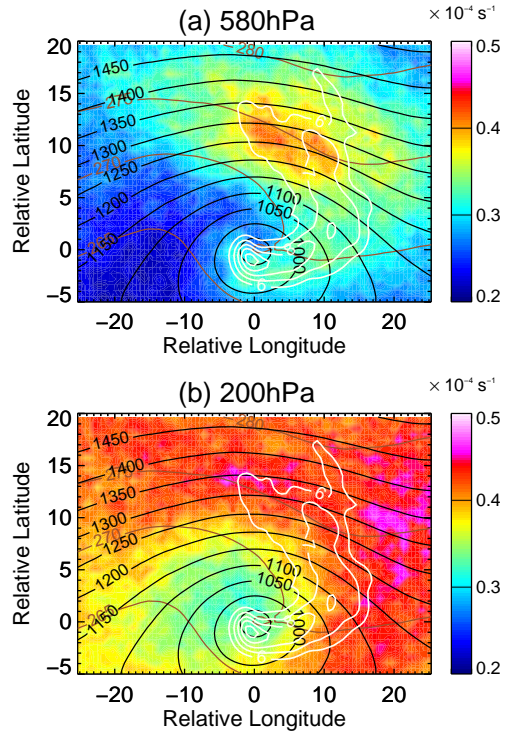


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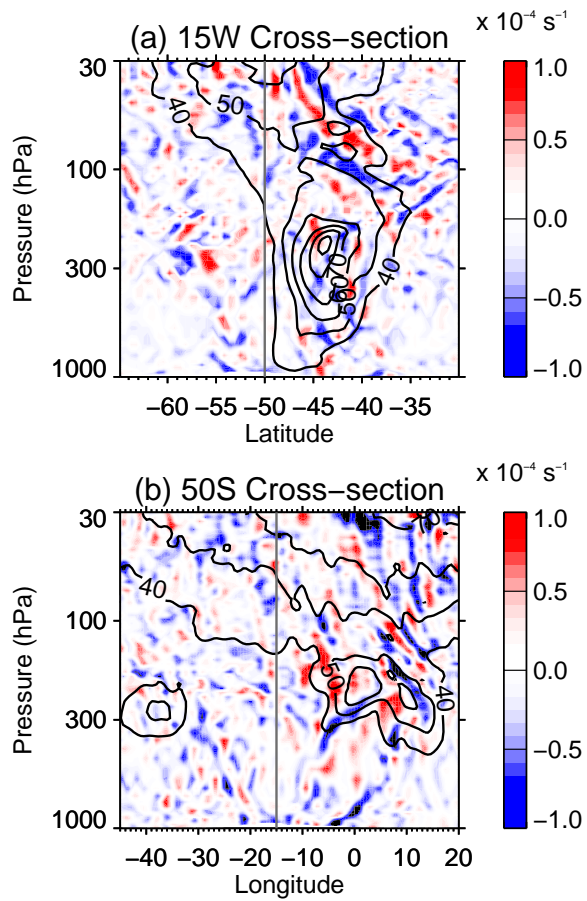


FIG. 12. Cross-sections in the South Atlantic of the horizontal wind divergence (color) and zonal wind (black lines, units of  $\text{m s}^{-1}$ ) through the center of a depression at (a)  $15^\circ\text{W}$  and (b)  $50^\circ\text{S}$ . Vertical gray lines indicate the cross-section for each other's panel.



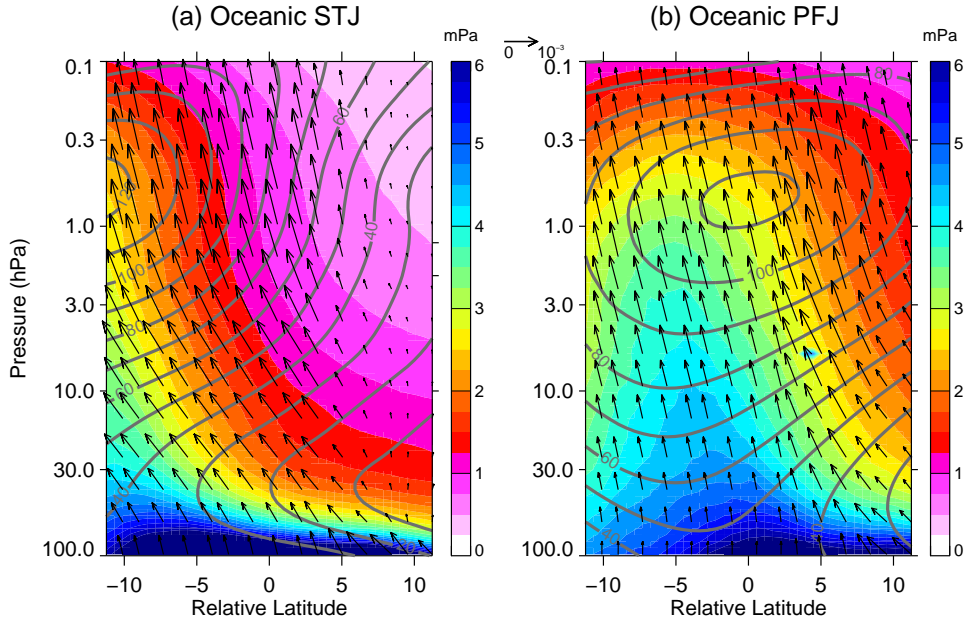


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